

Quiz 5 - PH242

Name _____

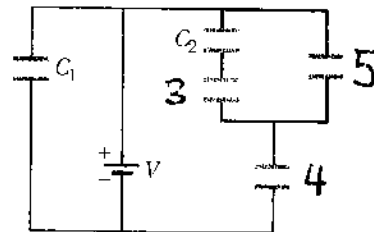
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In the figure below assume the battery has a potential difference of 10.0 V and all five capacitors shown have a capacitance of 10.0 μF .

(A) Calculate the equivalent (or total) capacitance for this circuit.

(B) Calculate the charge on C_1 .

(C) Calculate the charge on C_2 .



Equations

Three capacitors in

Series: $V = V_1 + V_2 + V_3$ $Q = Q_1 = Q_2 = Q_3$ $\frac{1}{C_{EQ}} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3}$

Three capacitors in

Parallel: $V = V_1 = V_2 = V_3$ $Q = Q_1 + Q_2 + Q_3$ $C_{EQ} = C_1 + C_2 + C_3$

$Q = CV$

(A) $\frac{1}{C_{23}} = \frac{1}{C_2} + \frac{1}{C_3} = \frac{2}{10\mu\text{F}} \Rightarrow \underline{C_{23} = 5\mu\text{F}}$

$C_{235} = C_{23} + C_5 = 15\mu\text{F}$ $\frac{1}{C_{4235}} = \frac{1}{C_4} + \frac{1}{C_{235}} = \frac{1}{10} + \frac{1}{15} = \frac{5}{30\mu\text{F}}$
 so $\underline{C_{4235} = 6\mu\text{F}}$

$C_{12345} = C_1 + C_{4235} = \boxed{16\mu\text{F}}$

(B) $C_1 = \frac{Q_1}{V_1}$ so $Q_1 = (16\mu\text{F})(10\text{V}) = 100\mu\text{C} = 100\mu\text{C}$
 $\boxed{= 1 \times 10^{-4} \text{C}}$

(C) $V_4 + V_{235} = 10\text{V}$, $V_2 = V_3 = V_{23}/2$, $Q_4 = Q_{235}$, $Q_2 = Q_3 = Q_{23}$

so $C_{235}V_{235} = C_4V_4$, $\frac{V_{235}}{V_4} = \frac{C_4}{C_{235}} = \frac{10\mu\text{F}}{15\mu\text{F}} = \frac{2}{3}$, $V_4 + \frac{2V_4}{3} = 10\text{V}$

~~so $V_4 = 6\text{V}$, $V_{235} = 4\text{V}$, $V_2 = V_3 = 2\text{V}$, $V_5 = 4\text{V}$ so $Q_2 = C_2V_2 = 20\mu\text{C}$~~

$V_4 = 6\text{V}$, $V_2 = V_3 = 2\text{V}$, $V_5 = 4\text{V}$ so $\boxed{Q_2 = C_2V_2 = 20\mu\text{C}}$